

$$2+2+2+1+2+2 = 11/12$$

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6.002 PS3

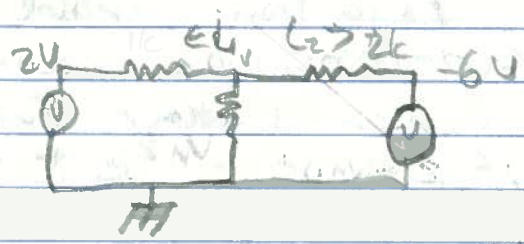
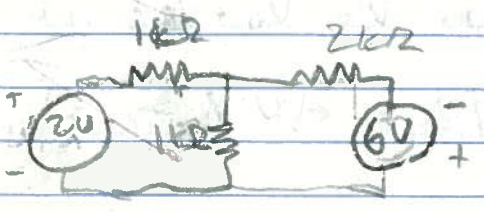
The two networks are linear, so their Thevenin equivalents can be found from the graph.

$$V_{TH1} = V_{oc1} = 2V \quad I_{N1} = I_{sc1} = 2mA$$

$$\Rightarrow R_{TH1} = \frac{V_{TH1}}{I_{N1}} = 1k\Omega$$

$$V_{TH2} = V_{oc2} = -6V \quad I_{N2} = I_{sc2} = 3mA$$

$$\Rightarrow R_{TH2} = \frac{V_{TH2}}{I_{N2}} = 2k\Omega$$



$$(-2V)/1k\Omega + v_1/1k\Omega + (v_1 - 6V)/2k\Omega = 0$$

$$\Rightarrow 2(v_1 - 2V) + 2v_1 + v_1 + 6V = 0$$

$$\Rightarrow 2v_1 + 2v_1 + v_1 = 4V - 6V$$

$$\Rightarrow v_1 = v_2 = -2/5V$$

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$$(-2/5V)(2V) \cdot 1k\Omega \Rightarrow$$

$$(2/5V - 6V) = v_2 \cdot 2k\Omega \Rightarrow$$

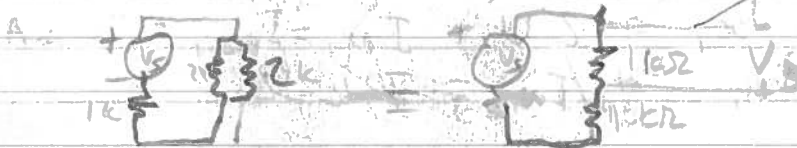
$$= -12/5V / 1k\Omega$$

$$= -2.4mA$$

$$= 2.8mA$$

2. a. w/ $V_s = 0$, the circuit is 3 parallel resistors w/ $R_{eq} = 2k\Omega // 1k\Omega // 2k\Omega = 500\Omega$, $V_A = I_s R_{eq} = 2mA \cdot 500\Omega = 1V$

w/ $I_s = 0$, the circuit is a series-parallel combo



By the voltage-divider relation $V_B = -V_s/2 = -2V$

By superposition, $V = V_A + V_B = 1V - 2V = -1V$

b. $P = IV = V^2/R = 1V^2/2k\Omega = 1/2 mW$

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Using the relation above, $P = V^2/R$, superposition cannot apply. Power is a non-linear function. $P = (V_A + V_B)^2/R$, not $V_A^2/R + V_B^2/R$

3a. $I_s = V_0/R + 2V_0/1k = V_0/1k + 2V_0/1k = 3V_0/1k$
 $5mA = V_0/1k + 2V_0/1k \implies (V_0 = 1.516V)$

b. $V_0 \approx 1.516V$

c. $L_D = V_0^3 + 3V_0^2 v_0$

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$L_S = L_R - L_D = 0$

$\Rightarrow I_s + L_S - V_0/1k - 2V_0/1k - V_0^3 - 3V_0^2 v_0 = 0$

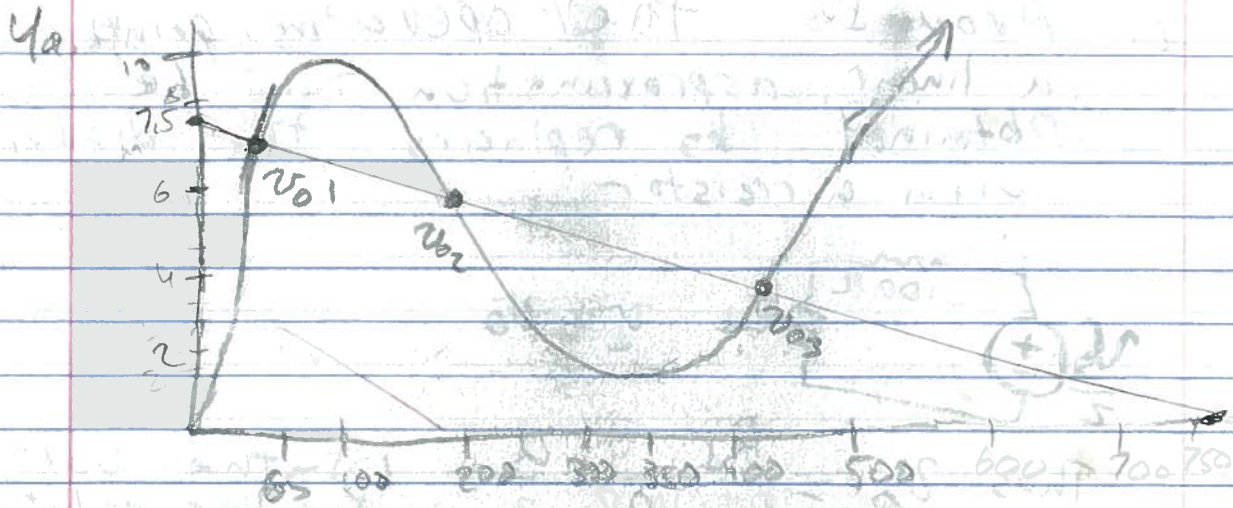
$\Rightarrow (I_s - V_0/1k - 2V_0/1k) + L_S - V_0^3 - 3V_0^2 v_0 = 0$

$\Rightarrow 0 + L_S - V_0/1k - 3V_0^2 v_0 = 0$

$\Rightarrow L_S = V_0 (1/1k + 3V_0^2)$

$\Rightarrow L_S = V_0 (1/1k + 3 \cdot (1.516V)^2)$

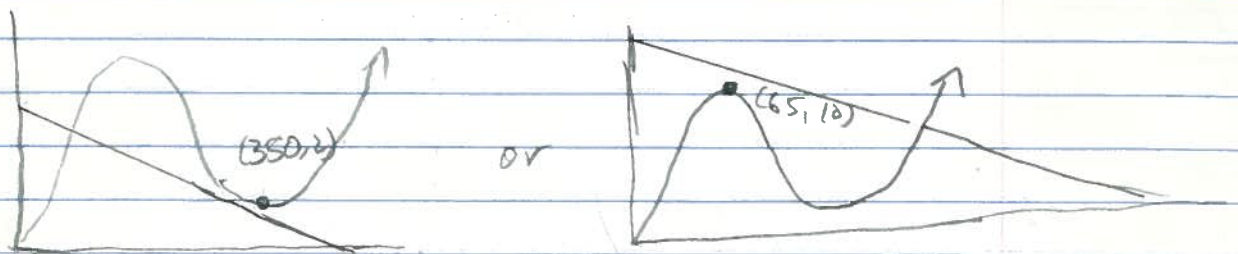
$\Rightarrow V_0/L_S = 1 + 3(1.516)^2 = 7.895$



The Thevenin open circuit voltage (V_{oc}) at the diode's terminals is $V_s/2 \approx 750 \text{ mV}$, and the Thevenin resistance is $100 \Omega \Rightarrow I_{sc} = 7.5 \text{ mA}$

From the graph, operating values exist at about $V \approx 50 \text{ mV}$, $I \approx 7 \text{ mA}$, $V \approx 200 \text{ mV}$, $I \approx 5.5 \text{ mA}$, $V \approx 450 \text{ mV}$, $I \approx 3.5 \text{ mA}$

b. Multiple solutions exist when the load line intersects the nonlinear curve in more than one place. In addition to the graph drawn above, adjusting V_s can give curves that look like:



when $I_{sc} = 350 \text{ mV} / 100 \Omega = 3.5 \text{ mA}$... $I_{sc} = 65 \text{ mV} / 100 \Omega > 10 \text{ mA}$

$\Rightarrow V_s / 2 / 100 \Omega = 350 \text{ mV} / 100 \Omega = 3.5 \text{ mA}$ $V_s / 2 / 100 \Omega = 65 \text{ mV} / 100 \Omega > 10 \text{ mA}$

$\Rightarrow V_s = 700 \text{ mV} < 400 \text{ mV}$ $V_s = 130 \text{ mV} > 20 \text{ mV}$

$V_s < 400 \text{ mV} + 700 \text{ mV}$ $V_s < 20 \text{ mV} + 130 \text{ mV}$

$V_s < 1.1 \text{ V}$ $V_s > 2.13 \text{ V}$

Thus there are multiple solutions for $1.1 \text{ V} < V_s < 2.13 \text{ V}$ (approximately)

1. Around V_D , the v_D operating points a linear approximation can be obtained by replacing the diode with a resistor.



Thus $V_D = \frac{R_d}{R_d + 100\Omega} \frac{V_s}{2}$ by the voltage divider relationship

$$\Rightarrow \frac{V_D}{V_s} = \frac{R_d}{2R_d + 100\Omega}$$

where R_d is the equivalent resistance for small signal components, given by

$R_d = \frac{dv_D}{di_D}$ the reciprocal of the slope of the v_D curve at an operating point.

At $V_D = 0.7$ V, $i_D = 10$ mA, $r_D = 25$ mV / 10 mA = 2.5 Ω



$V_s = 10$ V
 $R_s = 100\Omega$
 $V_D = 0.7$ V
 $i_D = 10$ mA
 $r_D = 25$ mV / 10 mA = 2.5 Ω
 $V_{out} = \frac{2.5}{2 \times 2.5 + 100} \times 5 = 0.125$ V

A	B	C	D	O ₁	O ₂
0	0	0	0	0	0
0	0	0	1	0	0
0	0	1	0	0	0
0	0	1	1	0	0
0	1	0	0	0	0
0	1	0	1	0	0
0	1	1	0	0	0
0	1	1	1	0	0
1	0	0	0	0	0
1	0	0	1	0	0
1	0	1	0	0	0
1	0	1	1	0	0
1	1	0	0	0	0
1	1	0	1	0	0
1	1	1	0	0	0
1	1	1	1	0	0

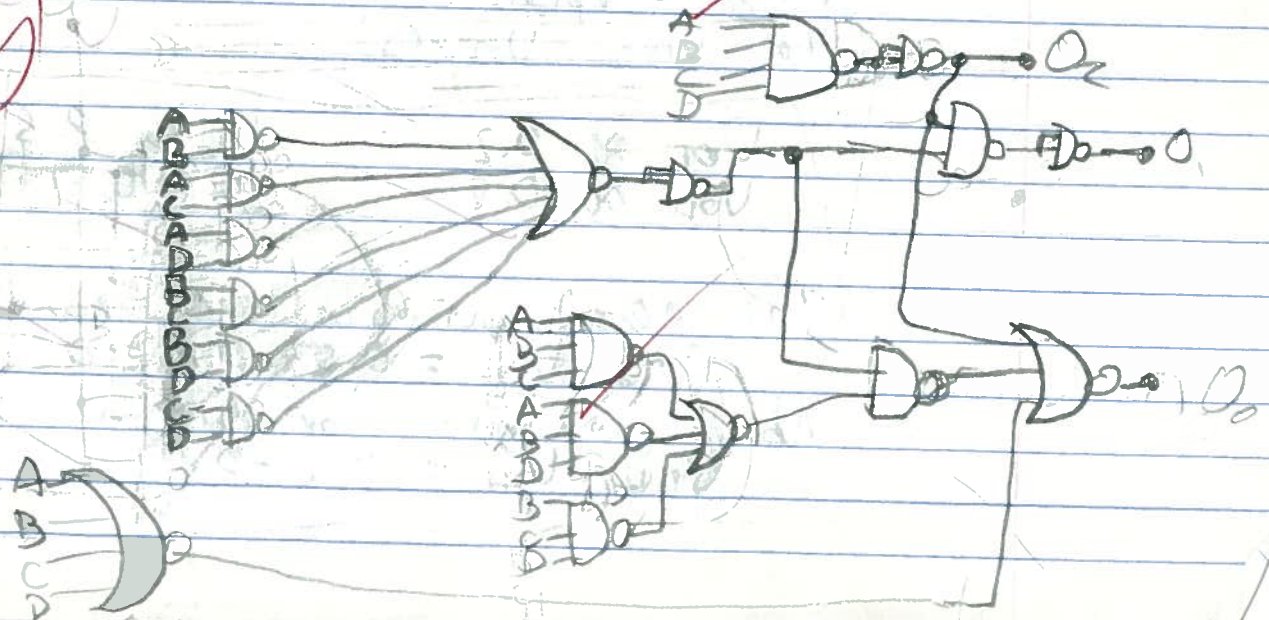
b)

$$O_2 = ABCD$$

$$O_1 = \bar{A}\bar{B}CD + \bar{A}B\bar{C}D + \bar{A}BC\bar{D} + \bar{A}BCD + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD + AB\bar{C}\bar{D} + ABC\bar{D}$$

$$O_0 = \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}BC\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D} + AB\bar{C}\bar{D} + ABC\bar{D}$$

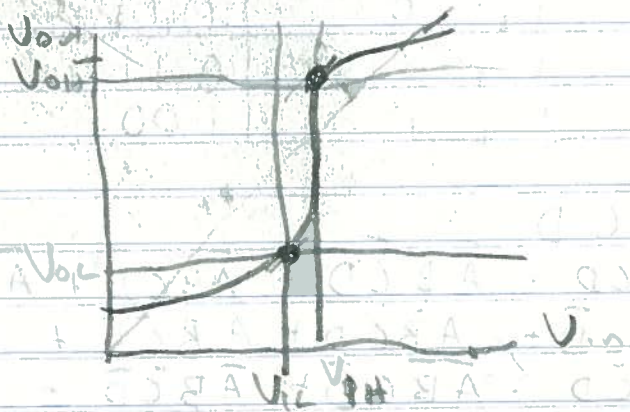
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6.a. To have no noise margin, $V_{OL} = V_{IL} = V_{IH} = V_{OH}$. This can only work when the curve intersects the $V_{out} = V_{in}$ line. This happens at about $V_{in} = V_{out} = 0.65V$.

Thus, $V_{OL} = V_{IL} = V_{IH} = V_{OH} = 0.65V$

6. The noise margin is $V_{IL} - V_{OL}$ or $V_{OH} - V_{OH}$. This is maximized when the curve is as far away from the $V_{out} = V_{in}$ line as possible, i.e., when the slope of the curve is 1.



This happens at approximately the following values:

$V_{OL} \approx 0.2$ $V_{IL} \approx 0.5$
 $V_{OH} \approx 0.8$ $V_{IH} \approx 0.7$

The noise margin for low value $V_{IL} - V_{OL} = 0.5 - 0.2 = 0.3$
 Noise margin for high value $V_{OH} - V_{IH} = 0.8 - 0.7 = 0.1$